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“ The next great era of awakening of human intellect may well produce a method of understanding the qualitative content of equations ” FEYNMAN