## CHAPTER IV

## THE INDUCTIVE JUSTIFICATION OF INDUCTION

The inductivists are not satisfied with an `analytic justification of induction'; because it does not give any induction will often assurance that lead to success. Inductivists argue that induction is a reliable guide for our expectations because it has worked well so far. of justification is called inductive justification of because it holds that the argument from `induction has worked in the past' to 'induction will work in the future' is a correct inductive inference.

Hume claims that inductive justification of induction circular because induction is relied upon in order to prove that induction is reliable. The proponents of inductive justification of induction point out that it is not circular in the ordinary sense because its conclusion is not one of the premisses from which the conclusion is derived. Actually an inductive justification of induction is circular in the sense that the conclusion asserts the correctness of the rule of inference bу which it is reached. The Inductivists claim that this kind οf circularity is not vicious and it does not spoil the cogency an argument.

Inductive justification of induction was first explicitly proposed by C. S. Peirce; later R. B. Braithwaite and Max Black have both championed this view. They maintain that induction could be inductively justified instead of being deductively justified by confirming to a rule or a standard of induction. The reason for accepting the inductive conclusion is that it has proved successful in the past, for example, we accept the conclusion "All men are mortal" on the basis that men have been proved mortal in the past. The inductivists say that there is a good reason why we should trust the inductive conclusion in question.

C. S. Peirce considers induction as a trustworthy method for pursuing truth due to its being a self-correcting process. He holds that in the case of inductions (synthetic inference) as distinguished from deduction (analytic inference) "We only know the degree of trustworthiness of our proceedings. As all knowledge comes from synthetic inference, we must equally infer that all human certainty consists merely in our knowing that the processes by which our knowledge has been derived are such as must generally have led to true conclusions". This type of argument amounts to an inductive justification of induction.

Peirce asserts that if induction is valid at all, its validity must consist in the fact that "it pursues a method which, if duly persisted must, in the very nature of things lead

to a result indefinitely approximating to truth in the long run".  $^{2}$ 

But here the question may arise as to how induction must in the long run lead to truth. Peirce may reply that induction is a method which always corrects its errors and leads us in reaching the true conclusion. Thus he argues "The true guarantee of the validity of induction is that it is a method of reaching conclusion, which if it be persisted in long enough, will assuredly correct any error concerning future experience into which it may temporarily lead us". 3

Peirce in his last writings asserts self-corrective tendency of induction as the heart and essence of inductive method. Induction is self-corrective if its conclusions are correlated by other such conclusion. One inductive conclusion corrects another if we reject one in favour of the other, because the sample on which the first conclusion based is larger than the sample on which the second conclusion is based.

Peirce concludes that "......the method of induction must generally aproximate to the truth; that is a sufficient justification for the use of the method, although no probability attaches to the inductive conclusion". Peirce's account of trustworthiness of inductive inference as the criterion of its validity makes inductive validity on the basis of some objective

fact about the principle, according to which the inference is made. Braithwaite objects that "............................... make this dependence a dependence upon the proportion of inference covered by the policy which lead to true conclusion is to put it in a form which is, in two ways badly suited for our purpose. In the first place, since the conclusion of an induction is a general hypothesis, there is no time at which it is conclusively proved. The hypothesis may, of course, be established by the induction, but its establishment at one time will not prevent its refutation at a later time if contrary evidence occurs".

Braithwaite considers that an inductive policy could be expected to be objective in the future if it has the character of being effective-in-the-past. In this sense the inductive principles, that whenever known members of a class are found to possess a certain character, it is probable that all members of the class possess that character is a valid one, if it has proved to be true and successful in most cases in the past.

Our inductive conclusions are to be considered as valid in accordance with the principle of Induction. But as soon as the objection that there is no logical reason for accepting this rule as a valid one is raised, this principle must be justified by itself in the sense that most of its applications in specific cases have been successful in the past. Braithwaite has proposed this way of justifying induction.

He believes that induction is not a demonstrative form of inference like deduction. Here he uses the word 'Induction' the sense in which it covers the inferences of an empirical generalization from its instances or of a scientific hypothesis from empirical evidences for it. Braithwaite asserts that belief in the premisses by itself does not generate belief in the conclusion and the reasonableness of belief in inductive conclusion requires fulfilment of more conditions than that reasonable belief in the premisses. It is also necessary that the conclusion is derived in accordance with a (valid) principle of inference. If in the inference one is aware of the validity of the principle besides having reasonable belief in the premisses, then the inference may be said to be subjectively valid. the conclusion is drawn from reasonably believed premisses without awareness of the valid principle of inference, then the inference is said to be objectively valid.

Braithwaite starts his considerations of justification of induction by saying that "all the inductions whose validity we wish to establish are inferences in which the inductive conclusion has been derived from the empirical premisses accordance with one or the other of a limited number of inductive principles of inference". 6 He claims that "the justification for inductive inference from known empirical data, i.e. the criterion for the `validity' of the inference and for the `reasonableness' of belief in the hypothesis which the conclusion of the induction, lies in the principle in accordance with which the inference is made being one of the policy of using which has a charateristic, which I shall call "predictive reliability" and which C. S. Peirce once called "truth producing vitrue".

According to Braithwaite, the justification of induction consists in the fact that a policy of passing according to an inductive principle from true beliefs to beliefs-in-general hypothesis frequently enables us to accept hypothesis which are confirmed and unrefuted by experience.

Braithwaite begins his argument by defining an inductive policy as a policy "for establishing general hypothesis in accordance with inductive principles of inference on the basis of empirical data".

He suggests the following criterion for the "reliability" of an inductive policy II and for the validity of any inference, reasonableness of belief in any hypothesis it sanctions. (Inductive policy II is represented by a greek capital letter which denotes only the simple enumerative inductive policy).

"Of every time  $\underline{t}$  later than a fixed time  $\underline{t}$ , and of every interval of time of a fixed length of years,  $\underline{d}$  lying within the interval ( $\underline{t}$ 0,t), it is true that many of the hypotheses

established by the use of policy II during the interval of  $\underline{d}$  years (unless there is no such hypotheses) have the joint property (1) of not having been empirically refuted at any time between the time of establishment and  $\underline{t}$ , (2) of having been empirically confirmed atleast once between the time of establishment and  $\underline{t}$ .

The important point is that for a policy II to be reliable it must have what Peirce called "truth producing virtue". Following his explication of this Peircean notion, Braithwaite defines an effective policy as one shich satisfies the criterion of reliability, and an effectiveness in the past policy as one which satisfies the criterion which results when "of every time t not later that the present time and substituted in the above for, of every time t". He assumes that "the effectiveness of an inductive policy is an empirical proposition which does not logically follow from the policy's effectiveness in the past". 10

Braithwaite tries to show that non-circularity (in the vicious sense) of the following argument 'A' justifying the use of the policy of simple enumeration. Argument 'A': (1) Policy II is effective in the past.

## Therefore:

(2) Policy II is effective. Braithwaite considers that an argument A obviously does not have among its premisses

principii sense of professing to infer a conclusion from a set of premisses, one of which is the conclusion itself". Braithwaite himself concedes that by this observation it is difficult to get rid from the charge of circularity. "Still there is the difficulty involved in the use of an inferential policy to establish its own effectiveness". 11 To overcome this difficulty Braithwaite proceeds to argue that argument 'A' is reasonably believed and the argument will be both valid and exempt from the charge of circularity if any of the following conditions are fulfilled.

- I 'Policy II is effective' is merely believed (and not reasonably believed) or
- II 'Policy II is effective' is true.
- III It is both believed (though not reasonably believed) and true.

Braithwaite uses the word 'valid' and 'validity' in the sense that "the conclusion can justifiably be added to the inferer's body of reasonable beliefs". Braithwaite says that all that is required for inferential validity in addition to the reasonable belief in the premisses of the argument is the truth of the proposition asserting the effectiveness of the principle governing the inference.

Braithwaite says that the person making the inference can be regarded simply as a reasoning machine. He says, "there is nothing objectionable in the machine arriving at a new proposition which corresponds to having a reasonable belief in a proposition asserting some general property of the method of working of machine". 13

Braithwaite gives an analogy between 'machine' and 'human being'. A machine could be constructed in such a way that when "fed" certain propositions it would arrive at the proposition that its "principle of working" was effective. There is nothing objectionable in the conception of such an occurence. Man, like can thus arrive from premisses to conclusion automatically. But human beings are unlike machines. A man believe or disbelieve or doubt; machines cannot. One feature οf this disimilarity is the human ability to question the status belief inferred from reasonably believed premisses by principle inference whose effectiveness is not similarly reasonably believed.

After developing the machine analogy Braithwaite writes "But if the machine becomes self conscious and critical of its mode of working, it will not be satisfied with a criterion for the validity of inference which depends upon the effectiveness in fact of the method by which it is working but will demand a condition either as an alternative or as an addition, which

## states its belief in this effectiveness". 14

He claims that it is sufficient for the validity of an inductive argument that the inference have reasonable belief in the premisses of the argument together with belief, though not reasonable belief, in the effectiveness of the principle of inference employed.

It is argued that belief in the proposition 'e' that a certain inferential 'policy II is effective' is "self-rationalizing, not of course in the sense that believing e makes this belief itself reasonable, but in the sense that believing e carries along with it a belief that this belief in e is reasonable". Braithwaite gives an argument as follows: From these premisses:

- (1) B reasonably believes the Policy II evidence for e
- (2) B believes e
- (3)  $\underline{e}$  is true. This conclusion can be drawn that it is both subjectively and objectively reasonable for B to believe e.

Braithwaite asserts that B has a reasonable belief in <u>e</u>, where <u>e</u> is a proposition asserting the effectiveness of using the principle. But the question arises that how can B arrive at a reasonable belief in <u>e</u>. Neither B arrives at a reasonable belief in e by direct observation nor indirectly because the criterion

of effectiveness refers to all time  $\underline{t}$  later than  $\underline{t}_{\underline{o}}$ , and hence also the future times. Therefore  $\underline{e}$  is a contingent proposition. Consequently his reasonable belief in  $\underline{e}$  depends on the use of the inductive principle of inference.

Braithwaite tries to escape from this circularity by the following analysis. He asserts that the circularity resides in presupposing that B must have a reasonable belief in e in order to arrive at a reasonable belief in e. But does the validity of B's inference depend upon this presupposition? According to Braithwaite there are three possible fundamental criteria for judging whether B's use of the inductive principle of inference is valid.

- (1) B believes e
- (2) B has a reasonable belief in e
- (3)  $\underline{e}$  is true.

Braithwaite accepts that if B has a reasonable belief in e is the only acceptable criterion for validity, the inductive derivation of a reasonable belief in e would be circular. He claims that (1) 'B believes e' by itself establishes the "subjective validity" of B's use of the inductive principles of inference. (2) 'e is true' by itself establishes the 'objective validity' of his use of the principle. (3) The premiss 'B

believes e' and the conclusion 'e is true' together establish the subjective and objective validity of his use of the principle. The subjective validity and objective validity is a justification for B to make inference in conformity with the inductive principle of inference. Neither subjective nor objective validity assume that 'B has a reasonable belief in e'. Thus Braithwaite claims that there is no circularity in his use of the inductive principle of inference in reaching at a reasonable belief in e.

Abner Shimony refutes the above treatment of induction. He says "Prof. Braithwaite has gained no advantage by performing inductions in terms of rules of inference rather than in terms of supressed premisses, for an argument using a non-deductive principle of inference makes exactly the same assumptions as a corresponding argument in which the principle of inference is deductive but premisses are suitably strenghtened". 16

Braithwaite's attempts to avoid the circularity is refuted by Abner Shimony. He argues in the same article that the "subjective validity" of B's use of the inductive principle of inference does not make it reasonable for him to infer according to this principle, for his belief in its effectiveness may be ungrounded. Nor does "objective validity" make it reasonable for B to use the principle, unless he also knows or reasonably believes that it is objectively valid; otherwise the

correctness of his mode of inferring is merely a lucky guess. Finally, since both components are of so little help it is hard to see how the combination of "subjective and objective validity" can make B's use of the inductive principle of inference reasonable". 17

Although Braithwaite's arguments are powerful, yet we should still have a good reason for hesitating to accept his conclusion. In fact Braithwaite was unable to avoid the charge of circularity which is involved in inductive principle.

Max Black has been the staunchest supporter of the non-circularity of inductive justification of induction. According to him, to construct an inductive argument, supporting a principle of induction which avoids circularity, depends on the distinction between a premiss of an inference and a rule in accordance with which one infers. Many philosophers believe that there is a circulatiry in this assumption that what has already worked will continue to do so uses an inductive rule. Max Black claims that the appearance of circularity arises only from overhasty application of criteria applicable to deduction.

Max Black wants to establish the conclusion that `all inductive arguments are to be conducted according to one and the same inductive rule'. An inductive argument in support of that rule might be correct. He believes that conjunction of the

premisses and the negation of the conclusion is not self-contradictory. According to him this follows from the meaning of inductive argument that an inductive argument is not a special kind of deductive argument. Deductive arguments either establish their conclusion or they do not. On the other hand, an inductive argument may offer stronger or weaker reason in support of its conclusion. Black assumes that there is only one supreme inductive rule or principle which determines all correct inductive arguments and has to be shown to be true or probable. He formulates an example of self-supporting inductive argument. He believes that such self supporting-inferences may satisfy the conditions for legitimate inductive inference. The example is as follows:

" $R_1$ : To argue from all examined instances of `A's have been B 'to `all A's are B'.

 $R_2$ : To argue from: `most instance of A's examined in a wide variety of condition have been B' to `(probably) the next A to be encountered will be B'"

Further he says that we can formulate two inductive arguments for the support of rule  $R_1$  and  $R_2$  respectively.

"(a $_1$ ) All examined instances of the use of  $R_1$  in arguments with true premisses have been instances in which  $R_1$  has been

successful.

Hence

All instances of the use of  $R_1$  in the argument with true premisses are instances in which  $R_1$  is successful".

Black gives another argument in support of  $R_2$  "( $a_2$ ) In most instances of the case of  $R_2$  in arguments with true premisses examined in a wide variety of conditions,  $R_2$  has been successful.

Hence (probably)

In the next instances to be encountered of the use of  $R_2$  is an argument with true premisses  $R_2$  will be successful".  $^{18}$ 

The argument  $a_1$  is governed by  $R_1$  and  $a_2$  by  $R_2$  (In Black's 'Self Supporting Inductive Argument( $a_2$ ) is called (a) and  $R_2$  is called (R).)

Max Black calls (a<sub>1</sub>) argument the first order argument and (a<sub>2</sub>) the second order argument. According to him the word 'probably' here indicates the 'variability of strength' of these arguments. He claims that this argument cannot be circular since its conclusion is not one of its premisses, or even hidden in one of its premisses. The conclusion does not follow deductively from the premisses. Though this would not be good for a deductive argument but it saves our inductive argument from

circularity. The argument may also be "Correct without triviality".

Max Black argues that 'Variability in strength' is important for inductive arguments. By the help of this we can distinguish inductive argument from deductive ones. A deductive rule is either valid or invalid but in inductive rule 'degree of reliability' depends upon its ratio of success it assumes in previous applications. Black says that the measure of the strength of an argument is m/n; that is, relative frequency of the successful applications of the argument with true premisses.

"Suppose evidence is available that 4/5 of the A's so far examined have been B, and it is proposed by an application of the rule R, to draw the inference that the next A to be encountered will be B. Suppose for the sake of argument we know R to have been successful in 9/10 of the cases in which it has been previously used. If so, the second order argument affirms with strength 9/10 that R will be successful in the next instance of its use. Thus there is a transfer of the strength from the second order argument to the first order argument". 19

In arguing that the second order argument  $(a_2)$  supports the rule  $R_2$ , Black is claiming that the strength of the argument raises the degree of reliability of the rule.

Black attempts to show that if all goes well inductive method becomes self-regulating and self-supporting. According to him "If we have no reason to think that R is unsuccessful most of the time, or is objectionable on some logical grounds, that is enough to make our employment of it so far reasonable. The function of higher order arguments in the tangled web of inductive method is to permit us to progress from relatively imprecise and uncritical methods to methods whose degrees of reliability and limits of applicability have themselves been checked by inductive investigations". 21

evidence against the conclusion or as no evidence either positive or negative. To regard the fact in the premisses as evidence for the conclusion is to assume that the rule of inference used in the argument is a correct one. And this is precisely what is to be proved. If the conclusion is denied then the facts stated in the premisses are no longer evidence for the conclusion". 22

Black argues that Salmon's views are improper because `conclusiveness' can be used for deductive argument but not for an inductive argument. An inductive argument may be correct Black claims that Salmon is making a mistake incorrect. bу saying that the falsity of (a)'s conclusion entails the incorrectness of the rule by which (a) is governed. Black further argues that "He (Salmon) would be plainly wrong if hе maintained that an assertion of the correctness of (a) was an additional premiss required by (a), or that an argument the effect that (a) was correct must precede the legitimate For if this last demand were pressed it would render deductive inference no less than inductive inference logically impossible. If we were never entitled to use a correct rule inference before we had formally argued in support of that rule, the process of inference could never get started". 23

He claims that if there is such a thing as inductive correctness and if its instances can be experienced before then there are cirteria of inductive correctness which can be found as

vindicated. According to Salmon, it is a gross mistake to say that "a given inductive rule can be established by a self-supporting argument". According to Black "if `established' means the same as `proved reliable', the self-supporting argument can strengthen the rule and in this way `support' it". 24

Peter Achinstein also gives two objections to the cogency of Black's argument. First he gives a counter-example and considers the rule of inference D: "Argue from 'No F is G': and "Some G is H' to the conclusion 'All F is H'".

Now the `self-supporting' argument (b) can be formulated as follows:

"premiss: No argument using D as its rule of inference is an argument which contains a premiss beginning with the term `All'; some arguments containing premisses beginning with the term `All' are valid.

Conclusion: All argument using D as their rule of inference are valid".  $^{25}$ 

Here in the self-supporting argument (b) neither its conclusion is the same as premisses nor it is presupposed by them. There is a similarity of structure. In the inductive case we know that the rule of inference is good, that is we have "subjected it to scrutiny" and so on, but in the above case we

know that the rule of inference is not good.

According to Achinstein this makes (a) circular. He says that in using the argument (a) to show that its conclusion is probable one must assume that its rule of inference is correct. And this involves the assumption that its conclusion is probable and thus there is a circularity.

Black maintains that the conclusion of (a) is that `R will be successful in its next application' and this is very different from the assumption that `R will probably be successful'.

Achinstein is not satisfied with Black's argument. He argues that what possible ground there can be for accepting the conclusion of the argument? He assumes that the only ground which can be given is that R is probably a generally successful rule. Black points out that R will probably be successful does

not entail that it will be successful on its next application. But Achinstein says that R's probable success provides the ground for accepting the conclusion of the argument (a). According to him there is a circularity. We cannot know the adequacy, the correctness of the rule of inference in accordance with which we construct the argument, without "simultaneously or antecedently".

Bredo C. Johnson also refutes Black's thesis. According to him it is impossible that the strength of an argument is completely independent of the degree of reliability of its rule. In fact their independence is essential to Black's argument; otherwise he could be committed to the view that one must take the rules of degree of reliability into account in determining the strength of an argument. But that having done so one can redetermine it with a different result by applying to the rules of the degree or reliability.

Further Johnson argues that "if the possiblity of an inductive justification of induction depends on the possiblity of increasing the strength of inductive arguments by means of second level arguments making use of the same inductive rule, then the former possiblity does not exist". 27

In this way inductive justification of induction is not able to dispose of the problem of induction. It also does not go to the roots of the philosophical perplexities. This inductive

justification of induction does not lead to any new solution or dissolution of the problem of justifying the inference. There are many problems in Inductivist's argument. However, they are useful in pin-pointing some difficulties in the justification of induction.