

## Contents

Certificate of the Supervisor	..... i
Acknowledgements	..... ii – iii
List of publications	..... iv – v
First page of publications	..... vi - xii
Contents	..... xiii - xv

### Chapter I

<b>Introduction</b>	<b>..... 1 - 12</b>
<b>1-1 Physical Background</b>	<b>.... 1</b>
<b>1-2 A few words about nonlinearity</b>	
1-2-1 : What is nonlinearity	.... 4
1-2-2 : Different approaches for understanding non-linearity	..... 6
1-2-3 : An introduction to Solitons	..... 9
1-2-4 : An introduction to Chaos	..... 10

### Chapter II

<b>The nonlinear field equations understudy and motivation for the study</b>	<b>..... 13 - 23</b>
2-1 : Yang Euclidean SU(2) R-gauge field equations	....14
2-2 : Charap Chiral field equations of pion dynamics	.... 18
2-3 : Motivation for the Combination of the Yang equations and Charap equations	.... 20
2-4 : Formulation of the Combined equations	... 22

### **Chapter III**

**Objectives of the present study ..... 24**

### **Chapter IV**

**Methodology used for the present study ..25 - 47**

4-1 : Ad-hoc procedure ..... 25

4-2 : Method of Graphical representations ..... 26

4-3 : Methodology for Painleve' test ..... 27

### **Chapter V**

**Review of the previous work related to the  
present study .....48 - 61**

#### **5-1: Review of Exact solutions**

5-1-1: Review of the exact solutions for the  
Yang equations ..... 48

5-1-2: Review of the exact solutions for the  
Charap equations ..... 54

#### **5-2: Review of Painleve' test**

5-2-1: Review of the Painleve' test for  
the Yang equations ..... 60

## **Chapter VI**

### **Present study for the three equations ...62 – 141**

#### **6-1 Study of exact solutions of three equations ... 62 - 129**

- 6-1-1 Some exact solutions of the Yang equations ....63  
 6-1-2 Some exact solutions of the Charap equations ...100  
 6-1-3 Some exact solutions of the Combined equations.118

#### **6-2 Graphical representation of some exact solutions for the three equations under study ....130 - 142**

- 6-2-1 Graphical representation of some exact solutions  
for Yang equations ... 131  
 6-2-2 Graphical representation of some exact solutions  
for Charap equations ....136  
 6-2-3 Graphical representation of some exact solutions  
for Combined equations ... 138

#### **6-3 Painleve' test of the three equations under study and discussion of chaos....143-189**

- 6-3-1: On a revisit to the Painleve' test for integrability  
and exact solutions for Yang equations ...144  
 6-3-2: Painleve' test for integrability and exact solutions  
for Charap equations ...163  
 6-3-3: Discussion on Painleve' test for integrability for  
Combined equations ... 176  
 6-3-4: Discussion of Chaos in the perspective of  
Painleve' test and Graphical representation  
of some exact solutions ...188

**Summary ..... 190**

**References ..... 196**

<p>“ The next great era of awakening of human intellect may well produce a method of understanding the qualitative content of equations ” ..... FEYNMAN</p>
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