## CHAPTER - 8

## CAUSAL RELATIONSHIP BETWEEN RUPEE/NEPALESE RUPEE EXCHANGE RATE AND RELATIVE PRICE LEVEL-A STUDY WITH VECTOR AUTOREGRESSIVE MODEL

### 8.1 Introduction:

'Cointegration' study in Chapter 6 has confirmed the existence of long-run relation between exchange rate $\left(e_{t}\right)$ and relative price level $\left(p_{t}\right)$ over the sub-period 1993:2-2006:1. The study with the estimated Vector Error Correction Model (VECM) in Chapter 7 has established the stability of such long run relationship between $e_{t}$ and $p_{t}$. It is, therefore, pertinent to examine if the estimated relationship between $e_{t}$ and $p_{t}$ or a variant of it could be effectively used for forecasting the future values of the variables concerned.

Granger and Newbold (1977) hold that any stable long-run relationship can be effectively used as a forecasting equation provided such relationship entails 'Causality' of any sort running from any of the variables to another. If $\mathrm{e}_{\mathrm{t}}$, in Granger's Sense, causes $\mathrm{p}_{\mathrm{t}}$, then the equation can be used to forecast future values of $\mathrm{p}_{\mathrm{t}}$. If, on the other hand, $\mathrm{p}_{\mathrm{t}}$, in Granger's Sense, causes $\mathrm{e}_{\mathrm{t}}$, then the equation may serve as an effective forecasting equation for $\mathrm{e}_{\mathrm{t}}$. If there exists bi-directional causality, in Granger Sense, then the equations can serve as the basis for the forecasting of both $e_{t}$ and $p_{t}$.

We, therefore, seek to examine, the nature and direction of Granger Causality between $\mathrm{e}_{\mathrm{t}}$ and $p_{t}$ in their long-run relationship over the sub-period 1993:2-2006:1, as evidenced by the study of Cointegration in Chapter 6. The study in this Chapter is devoted to address this issue. The study is carried through the estimation of an appropriate Vector Autoregressive Model (VAR) for $\mathrm{e}_{\mathrm{t}}$ and $\mathrm{p}_{\mathrm{t}}$ over the period 1993:2-2006:1.

### 8.2 The Vector Autoregressive (VAR) Model

The Vector Autoregressive (VAR) Model for Rupee/Nepalese Rupee Exchange Rate( $\mathrm{e}_{\mathrm{t}}$ ) and relative price level $\left(p_{t}\right)$ is as follows.

$$
\begin{align*}
& E_{1}=\alpha_{1}+\sum_{i=1}^{m} \beta_{1 i} E_{t-i}+\sum_{i=1}^{m} \gamma_{11} p_{t-i}+u_{11}  \tag{8.1}\\
& p_{t}=\alpha_{2}+\sum_{i=1}^{m} \beta_{2 i} E_{t-i}+\sum_{i=1}^{m} \gamma_{21} p_{t-i}+u_{21} \tag{8.2}
\end{align*}
$$

Here $E_{1}=\Delta e_{1}$ and $P_{1}=\Delta p$, represent the first differenced stationary time series dataset for $e_{t}$ and $p_{t}$ respectively over the sub-period 1993:2-2006:1. Since $e_{t} \sim I(1)$ and $p_{r} \sim I(1)$, the stationarity of $E_{t}$ and $P_{t}$ is ensured through the first difference filtering of $e_{t}$ and $p_{\mathrm{t}}$ respectively.
$u_{11} \sim G W N\left(0, \sigma^{2}{ }_{u_{1}}\right)$ and $u_{21} \sim G W N\left(0, \sigma^{2}{ }_{u_{1}}\right)$ are the stochastic error terms which are known as impulse or innovations or shocks in the VAR Model.

The equations (8.1) and (8.2) represent 'Seemingly Unrelated Regression Equations' (SURE) since the joint estimation of these equations considers and uses the 'Contemporaneous Var-Covariance matrix ( $\mathbf{\Omega}$ ) of the cross equation error terms involved such that $\boldsymbol{\Omega}=\operatorname{Var}-\operatorname{Covar}\left(\mathbf{u}_{\mathbf{1 t}}, \mathbf{u}_{\mathbf{2 t}}\right)$ where $\boldsymbol{\Omega}$ is a Positive Definite Matrix.

### 8.3 Selection of Lag Length in the VAR Estimation

The optimum lag length ( m ) has been determined on the basis of some Information Criteria like Akaike Information Criterion (AIC), Schwartz Information Criterion (SIC), Hannan-Quin Information Criterion (HQIC), Sequential Modified LR Test Statistic (SMLST), Forecast Prediction Error(FPE) Statistic etc. The Table 8.1.presents the relevant lag length statistics as given by these criteria.

## Table 8.1

## VAR LAG ORDER SELECTION CRITERIA

| Endogenous variables: $\mathrm{E}_{\mathrm{t}}, \mathrm{P}_{\mathrm{t}}$ Exogenous variables: C <br> Sample: $1993: 2$ 2006:1 <br> Included observations: 46 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Lag | LogL | LR | FPE | AIC | SIC | HQ |
| 0 | 321.8117 | NA | $3.14 \mathrm{E}-09$ | -13.905 | -13.825 | -13.875 |
| 1 | 328.3466 | 12.21741 | $2.81 \mathrm{E}-09$ | -14.015 | -13.776 | -13.926 |
| 2 | 339.0528 | 19.08504 | $2.10 \mathrm{E}-09$ | -14.307 | $-13.909^{*}$ | $-14.158^{*}$ |
| 3 | 339.3525 | 0.508246 | $2.48 \mathrm{E}-09$ | -14.146 | -13.589 | -13.937 |
| 4 | $\mathbf{3 4 6 . 4 0 2 0}$ | $\mathbf{1 1 . 3 4 0 3 7 ^ { * }}$ | $\mathbf{2 . 1 8 E - 0 9}$ | $-\mathbf{1 4 . 2 7 8}$ | $-\mathbf{1 3 . 5 6 3}$ | $\mathbf{- 1 4 . 0 1 0}$ |
| 5 | 352.4333 | 9.178141 | $2.01 \mathrm{E}-09^{*}$ | $-14.367^{*}$ | -13.492 | -14.039 |
| $*$ indicates lag order selected by the criterion |  |  |  |  |  |  |
| LR: sequential modified LR test statistic (each test at 5\% level) |  |  |  |  |  |  |
| FPE: Final Prediction Error |  |  |  |  |  |  |
| AIC: Akaike Information Criterion |  |  |  |  |  |  |
| SIC: Schwarz Information Criterion |  |  |  |  |  |  |
| HQ: Hannan-Quinn Information Criterion |  |  |  |  |  |  |

SIC and HQ statistics suggest for lag 2 as the optimum lag. However, the LR statistics suggest for lag 4 as the optimum lag. The trial and error estimations, as suggested by Enders, also conform lag 4 as the optimum lag. So in the VAR model, consisting of equations (8.1) and (8.2), the optimum lag (m) is set to be 4.

### 8.4 Results of the Estimation of the VAR Model

Results of the estimation of the VAR model are being presented through the Tables 8.2 and 8.3.

## Table : 8.2

## Results of VAR Model Estimation (Equation 8.1)

Sub-Period: 1993:2-2006:1 Sample (adjusted): 1994:3-2006:1
Included Observations: 47 (after adjusting endpoint)

| Dependent <br> Variable | Explanatory <br> Variable/Constant | Coefficient | S.E | t-stat. | Prob. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{E}_{1}$ | Constant | -0.001 | 0.001 | -0.876 | 0.386 |
|  | $\mathrm{E}_{\mathrm{t}-1}$ | -0.657 | 0.162 | -4.042 | 0.000 |
|  | $\mathrm{E}_{\mathrm{t}-2}$ | -0.456 | 0.194 | -2.348 | 0.024 |
|  | $\mathrm{E}_{\mathrm{t}-3}$ | 0.030 | 0.194 | 0.155 | 0.877 |
|  | $\mathrm{E}_{\mathrm{t}-4}$ | 0.014 | 0.163 | 0.088 | 0.930 |
|  | $\mathrm{P}_{\mathrm{t}-1}$ | 0.007 | 0.092 | 0.076 | 0.939 |
|  | $\mathrm{P}_{\mathrm{t}-2}$ | -0.109 | 0.090 | -1.216 | 0.232 |
|  | $\mathrm{P}_{\mathrm{t}-3}$ | 0.035 | 0.088 | 0.397 | 0.694 |
|  | $\mathrm{P}_{\mathrm{t}-4}$ | -0.202 | 0.087 | -2.332 | 0.025 |
| Log L | $\begin{aligned} & \mathrm{R}^{2}=0.433 \quad \text { Adj } \\ & \text { kelihood }=188.730 \end{aligned}$ <br> Determinant Resi | $\begin{aligned} & \mathrm{AIC}=-7.648 \text { SIC }=-7.294 \\ & \text { al Covariance }=1.46 \mathrm{E}-09 \end{aligned}$ |  |  |  |

## Table: 8.3

## Results of VAR Model Estimation (Equation 8.2)

Sub-Period: 1993:2-2006:1 Sample (adjusted): 1994:3-2006:1
Included Observations: 47 (after adjusting endpoint)

| Dependent <br> Variable | Explanatory <br> Variable/Constant | Coefficient | S.E | t-stat. | Prob. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{\mathrm{t}}$ | Constant | -0.000 | 0.001 | -0.157 | 0.876 |
|  | $\mathrm{E}_{\text {t-1 }}$ | 0.003 | 0.271 | 0.013 | 0.990 |
|  | $\mathrm{E}_{\mathrm{t}-2}$ | 0.102 | 0.324 | 0.314 | 0.755 |
|  | $\mathrm{E}_{\mathrm{t}-3}$ | 0.240 | 0.324 | 0.740 | 0.464 |
|  | $\mathrm{E}_{\mathrm{t}-4}$ | 0.410 | 0.272 | 1.509 | 0.139 |
|  | $\mathrm{P}_{\mathrm{t}-1}$ | 0.141 | 0.154 | 0.914 | 0.367 |
|  | $\mathrm{P}_{\mathrm{t}-2}$ | -0.225 | 0.150 | -1.497 | 0.143 |
|  | $\mathrm{P}_{\mathrm{t}-3}$ | 0.047 | 0.148 | 0.320 | 0.751 |
|  | $\mathrm{P}_{\mathrm{t}-4}$ | 0.432 | 0.145 | 2.986 | 0.005 |
| $\begin{aligned} & \mathrm{R}^{2}=0.396 \text { Adj } \mathrm{R}^{2}=0.269 \text { F-Stat. }=3.115 \\ & \text { ikelihood }=164.656 \text { AIC }=-6.624 \quad \text { SIC }=-6.269 \\ & \text { Determinant Residual Covariance }=1.46 \mathrm{E}-09 \end{aligned}$ |  |  |  |  |  |

### 8.5 Essential Features of the VAR Model

The VAR Model consisting of equations (8.1) and (8.2) requires that
i. $\quad \mathrm{E}_{\mathrm{t}}$ and $\mathrm{P}_{\mathrm{t}}$ be 'Stationary'.
ii. the model be 'Stable'.
iii. $\quad u_{1 t}$ and $u_{2 t}$ be white noise terms such that

$$
\begin{aligned}
& \boldsymbol{u}_{11} \sim i i d N\left(0, \sigma_{u_{1}}^{2}\right) \\
& \boldsymbol{u}_{2,} \sim i i d N\left(0, \sigma_{u_{2}}^{2}\right)
\end{aligned}
$$

In this model $E_{t}$ and $P_{t}$ are 'Stationary' since
$E_{1}=\Delta e_{1}$ and $P_{1}=\Delta p_{1}$
where $e_{t} \sim I(1)$ and $p_{t}=I(1)$
Therefore $E_{t} \sim I(0)$ and $P_{t}=I(0)$
Consequently, the first requirement is satisfied.
Again the consistence of the VAR Model requires that the model be stable. The conditions of 'stability' are derived below and then we proceed to examine if these conditions are met by the estimated VAR model. Once the 'stability' conditions are satisfied, then we would examine if $u_{1 t}$ and $u_{2 t}$ are white noise by nature.

### 8.6 Conditions of Stability For the VAR Model

From the equation (8.1) we have

$$
\begin{gather*}
E_{1}-\sum_{i=1}^{4} \beta_{1 i} E_{1-i}=\alpha_{1}+\sum_{i=1}^{+} \gamma_{2 i} P_{t-i}+u_{11} \\
\text { or } E_{1}\left(1-\sum_{i=1}^{4} \beta_{1 i} L^{\prime}\right)=\alpha_{1}+\sum_{i=1}^{4} \gamma_{2 i} P_{1-i}+u_{1 \prime} \\
\text { or } A(L) E_{1}=\alpha_{1}+\sum_{i=1}^{4} \gamma_{2 i} P_{t-1}+u_{11} \\
\text { or } E_{1}=[A(L)]^{-1}\left[\alpha_{1}+\sum_{i=1}^{4} \gamma_{2 i} P_{1-i}+u_{11}\right]  \tag{8.}\\
\text { where } A(L)=\left(1-\beta_{11} L-\beta_{12} L^{2}-\beta_{13} L^{3}-\beta_{11} L^{4}\right.
\end{gather*}
$$

The absolute value of each of the eigen values of the Characteristic Polynomial $\boldsymbol{A}(\boldsymbol{L})$ in equation (8.3) must be less than unity for the stability of the equation (8.1). Similarly, from the equation (8.2) we have

$$
P_{1}=[B(L)]^{-1}\left[\alpha_{2}+\sum_{i=1}^{4} \gamma_{2 i} E_{1,1}+u_{2,1}\right.
$$

where

$$
\begin{align*}
B(L) & =\left(1-\sum_{i=1}^{\dot{4}} \beta_{21} L^{\prime}\right) \\
& =\left(1-\beta_{11} L-\beta_{12} L^{2}-\beta_{13} L^{3}-\beta_{14} L^{4}\right) \tag{8.4}
\end{align*}
$$

The modulus of each of the eigen values of the Characteristic Polynomial $\boldsymbol{B}(L)$ in equation (8.4) must be less than unity for the stability of the equation (8.2). The roots of the AR characteristic polynomial $[A(L)$ or $B(L)]$ are being presented through the Table 8.4 while the Inverse Roots of AR characteristic polynomial $[A(L)$ or $B(L)]$ are shown by the Figure 8.1 below.

## Table 8.4

## VAR Stability Condition Check [Roots of the AR Characteristic Polynomial A(L)]

## Endogenous Variable: $E_{t}, P_{t}$

Exogenous Variable: C Lag Specification: 14

| Root | Modulus |
| :---: | :---: |
| $0.055132-0.888131 \mathrm{i}$ | 0.889841 |
| $0.055132+0.888131 \mathrm{i}$ | 0.889841 |
| $-0.303076-0.718820 \mathrm{i}$ | 0.780101 |
| $-0.303076+0.718820 \mathrm{i}$ | 0.780101 |
| $-0.640972-0.216865 \mathrm{i}$ | 0.676665 |
| $-0.640972+0.216865 \mathrm{i}$ | 0.676665 |
| $0.630875-0.079582 \mathrm{i}$ | 0.635874 |
| $0.630875+0.079582 \mathrm{i}$ | 0.635874 |
| No root lies outside the unit circle. |  |

Figure 8.1
Inverse Roots of AR Characteristic Polynomial A(L)


### 8.7 Examination of the Stability of the VAR Model

(A) The Table 8.4 presents the roots and respective modulus of each of the roots in A(L)

It is observed that
i. four of the eigen values are positive.
ii. four of the eigen value are negative.

Again the Figure 8.1 shows that inverse roots of the AR Characteristic Polynomial $\boldsymbol{A}(\mathbf{L})$ lie within unit circle. Thus the findings from the Figure 8.1 and the Table 8.4 confirm the 'Stability of the estimated VAR Model.

### 8.8 Normality of the VAR Residuals $u_{11}$ and $u_{2 t}$ : Jarque-Bera Test

Normality of the $\hat{u_{11}}$ and $\hat{u_{2 t}}$ is being examined through the Jarque-Bera VAR Residual Normality Tests. Results of such tests are being reported through the Table 8.5 below.

Table 8.5

## VAR Residual Normality Tests

Orthogonalization: Residual Correlation (Doornik-Hansen)
Null Hypothesis: residuals are multivariate normal
Sample: 1993:2-2006:1
Included observations: 47

| Component | Skewness | Chi-sq | df | Prob. |
| :---: | :---: | :---: | :---: | :--- |
| $\mathrm{E}_{\mathrm{t}}$ | -0.186 | 0.337 | 1 | 0.561 |
| $\mathrm{P}_{\mathrm{t}}$ | -0.026 | 0.007 | 1 | 0.935 |
| Joint |  | 0.344 | 2 | 0.842 |
| Component | Kurtosis | Chi-sq | df | Prob. |
| $\mathrm{E}_{\mathrm{t}}$ | 1.851 | 4.519 | 1 | 0.033 |
| $\mathrm{P}_{\mathrm{t}}$ | 1.276 | 20.364 | 1 | 0.000 |
| Joint |  | 2.632 | 2 | 0.000 |
| Component | Jarque-Bera | df | Prob. |  |
| $\mathrm{E}_{\mathrm{t}}$ | 4.856 | 2 | 0.088 |  |
| $\mathrm{P}_{\mathrm{t}}$ | 20.371 | 2 | 0.000 |  |
| Joint | 25.227 | 4 | 0.000 |  |

It is observed from the Table 8.5 that
i．the JB statistic for $\hat{u_{1 t}}=4.856$ ．It implies that the null hypothesis（i．e residuals $\hat{u_{1 t}}$ are normal）has been accepted even at $10 \%$ level．
ii．the JB statistic for $\hat{u_{2 t}}=20.371$ ．The null hypothesis that residuals $\hat{u_{2 t}}$ are normal has been accepted even at $1 \%$ level．
iii．the JB statistic for the joint test of normality of $\hat{u_{1 t}}$ and $\hat{u_{2 t}}=25.227$ ．The null hypothesis of normality for both $\hat{u_{1 t}}$ and $\hat{u_{2 t}}$ has been accepted at $1 \%$ level．

These findings confirm the multivariate normality of the residuals $\left(\hat{u_{1 t}}\right.$ and $\hat{u_{2 t}}$ ）of the VAR model consisting of equations（8．1）and（8．2）．

## 8．9 Serial Independence of the VAR Residuals $\left(\hat{u_{1 t}}\right.$ and $\left.\hat{u_{2 t}}\right)$

The correlograms of the VAR residuals $\hat{u_{1 t}}$ and $\hat{u_{2 t}}$ are given by the Figures 8.2 and 8.3 below．

Figure： 8.2
Correlogram of Residuals $\hat{u}_{1 u}$

| Included observatio | ： 47 |  | Sample： | 1993：2 | 2006：1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Autocorrelation | Partial Correlation | $A C$ | PAC | Q－Stat | Prob |
| 11 | 111 | 10.080 | 0.080 | 0.3231 | 0.570 |
| E | 1 | 20.044 | 0.037 | 0.4206 | 0.810 |
|  |  | 30.021 | 0.015 | 0.4444 | 0.931 |
| E |  | 4 －0．131 | －0．137 | 1.3698 | 0.849 |
| H | 1 | $5-0.118$ | －0．102 | 2.1371 | 0.830 |
|  | 1易 | 6 －0．208 | －0．189 | 4.5782 | 0.599 |
| $1 \quad 1$ | 1 ＇ 1 | 70.006 | 0.048 | 4.5806 | 0.711 |
|  |  | 8－0．287 | －0．309 | 9.4299 | 0.307 |
| 11 | 1 | $9-0.006$ | 0.016 | 9.4323 | 0.398 |
| 11 | 11 | $10 \quad 0.128$ | 0.074 | 10.447 | 0.402 |
| 1 | 1 | 110.052 | 0.024 | 10.617 | 0.476 |
| 10 | 18 | 120.079 | －0．045 | 11.032 | 0.526 |
| 1 | 1 | 130.024 | －0．027 | 11.072 | 0.605 |
| 1 | E | 140.038 | －0．056 | 11.175 | 0.672 |
| 1易 |  | $15-0.209$ | －0．192 | 14.320 | 0.501 |
| 15 | 15 | $16-0.108$ | －0．154 | 15.184 | 0.511 |
| 15 | 151 | $17-0.081$ | －0．087 | 15.685 | 0.546 |
| 18 | 11 | $18-0.099$ | －0．042 | 16.464 | 0.560 |
| 1 | 1 | 190.045 | 0.010 | 16.628 | 0.615 |
| 1 炜 | H | $20 \quad 0.153$ | 0.111 | 18.616 | 0.547 |

Figure： 8.3
Correlogram of Residuals $\hat{\boldsymbol{u}}_{2 \iota}$

| Included observations： 47 |  | Sample：1993：2 2006：1 |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Autocorrelation | Partial Correlation | AC PAC | Q－Stat | Prob |
| 1 目 | －1 | $1 \begin{array}{lll}1 & 0.193 & 0.193\end{array}$ | 1.8713 | 0.171 |
| 1 | 1 － | $20.190 \quad 0.158$ | 3.7169 | 0.156 |
|  | 151 | $3-0.014-0.081$ | 3.7272 | 0.292 |
| 1 1 | 1 | 4－0．201－0．232 | 5.9002 | 0.207 |
|  | － | 5－0．340－0．287 | 12.229 | 0.032 |
|  |  | $6-0.358-0.242$ | 19.428 | 0.003 |
| 1F1 | 4 | 7－0．219－0．077 | 22.186 | 0.002 |
| 1 | 1 | $8-0.031 \quad 0.069$ | 22.244 | 0.004 |
| 1 | 111 | 9 90．035－0．022 | 22.318 | 0.008 |
|  | 1 ｜ | $10 \quad 0.029-0.206$ | 22.370 | 0.013 |
| 且1 | 1 I | $110.226 \quad 0.010$ | 25.644 | 0.007 |
| 1 1 | 11 | $120.153 \quad 0.015$ | 27.191 | 0.007 |
| 1 1 | 1 | 130.1650 .089 | 29.033 | 0.006 |
| 1 | － | 14－0．061－0．156 | 29.292 | 0.010 |
| 1 回 |  | 15－0．059－0．132 | 29.542 | 0.014 |
| 11 | 1 | $\begin{array}{llll}16 & 0.140 & 0.297\end{array}$ | 30.996 | 0.013 |
| 18 | 11 | $17-0.113 \quad 0.035$ | 31.975 | 0.015 |
| 1 － | 18 | 18－0．107－0．130 | 32.880 | 0.017 |
| 1 | 11 | $19 \quad 0.033 \quad 0.033$ | 32.971 | 0.024 |
| 1 1 | $1{ }^{\text {a }}$ | 20－0．141－0．189 | 34.679 | 0.022 |

It is observed from the Figures 8．2－8．3 that
i．the corresponding ACFs of $\hat{u_{1 t}}$ and $\hat{u_{2 t}}$ are free from any from significant spikes in the spread of lags from one through twenty．
ii．the corresponding PACFs of the VAR residuals $\hat{u_{1 t}}$ and $\hat{u_{2 t}}$ are also marked by the absence of any significant spikes in lags 1－20．

These observations indicate that the VAR residuals are serially independent，given that quarterly data for $e_{t}$ and $p_{t}$ have been used for the estimation of the VAR model．

### 8.10 Further Confirmation of Serial Independence: Portmanteau Test

Serial independence of the VAR residuals, $\hat{u_{1 \prime}}$ and $\hat{u_{2 t}}$, has further been examined through the 'Portmenteau Tests'. Results of such tests have been presented through the Table 8.6 below.

Table 8.6
VAR Residual Portmanteau Tests for Autocorrelations
Null Hypothesis: No Residual Autocorrelations up to lag h
Sample: 1993:2-2006:1 Included observations: 47

| Lags | Q-Stat | Prob. | Adj Q-Stat | Prob. | df |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2.544469 | NA* $^{*}$ | 2.599783 | NA* $^{*}$ | NA $^{*}$ |
| 2 | 4.946730 | NA* $^{*}$ | 5.108812 | NA* $^{*}$ | NA $^{*}$ |
| 3 | 5.418701 | NA* $^{*}$ | 5.612963 | NA* $^{*}$ | NA* $^{*}$ |
| 4 | 8.013421 | NA** $^{*}$ | 8.449052 | NA* $^{*}$ | NA* $^{*}$ |
| 5 | 16.95295 | 0.0020 | 18.45281 | 0.0010 | 4 |
| 6 | 25.12574 | 0.0015 | 27.82162 | 0.0005 | 8 |
| 7 | 29.29382 | 0.0036 | 32.71911 | 0.0011 | 12 |
| 8 | 33.71842 | 0.0059 | 38.05132 | 0.0015 | 16 |
| 9 | 36.17345 | 0.0147 | 41.08781 | 0.0036 | 20 |
| 10 | 38.68280 | 0.0295 | 44.27536 | 0.0071 | 24 |
| 11 | 47.93089 | 0.0109 | 56.34925 | 0.0012 | 28 |
| 12 | 50.61613 | 0.0194 | 59.95515 | 0.0020 | 32 |

The Table 8.6 shows that
i. the adjusted Q -statistics in the Portmenteau Tests for lag $\mathrm{h}(4<h \leq 12)$ are significant even at $1 \%$ level.
ii. the null hypothesis of 'no residual autocorrelation' up to lag $h(4<h \leq 12)$ therefore, has been accepted at $1 \%$ level.

Thus the Portmenteau Tests also confirm serial independence of the VAR residuals ( $u_{17}$ and $\hat{u_{2 t}}$ ).

### 8.11 Homoscedasticity of the VAR Residuals $\left(\hat{u_{1 t}}\right.$ and $\left.\hat{u_{2 t}}\right)$

Time plots of the VAR residuals ( $\hat{u_{11}}$ and $\hat{u_{21}}$ ) are given by the Figures 8.4 and 8.5 respectively.

Figure: 8.4
Time Plot of VAR Residuals $\boldsymbol{U}_{1 t}$


Figure : 8.5
Time Plot of VAR Residuals $\hat{\boldsymbol{u}}_{2 t}$


The Figures 8.4 and 8.5 show that
i. time plots of $\hat{u_{1 \prime}}$ and $\hat{u_{2}}$, exhibit variations around 'zero' mean.
ii. $\hat{u_{11}}$ exhibits almost uniform variations around the zero-mean over the period concerned.
iii. time plot of $\hat{u_{2}}$, is devoid of any flutter or concentration of variations at or around any period.

All these observations testify for the 'homoscadasticity' of the VAR residuals $\hat{u_{11}}$ and $\wedge$
$u_{2 \prime}$.

### 8.12 Further Confirmation of Homoscdasticity of VAR Residuals: Correlogram of VAR Residual Variance

The homoscadasticity of VAR residuals $\hat{u_{1}}$, and $\hat{u_{21}}$ has further been examined through the study of the correlograms of the variance of the residuals concerned. The relevant correlograms are given by the Figure 8.6 and 8.7.

Figure： 8.6
Corrëlogram of Variance of VAR Residuals， $\boldsymbol{u}_{1 t}$

| Included observations： 47 |  |  | Sample：1993：2 2006：1 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Autocorrelation | Partial Correlation |  | $A C$ | PAC | Q－Stat | Prob |
| 1 | 1 | 1 | 0.463 | 0.463 | 10.744 | 0.001 |
| 1 | 1 | 2 | 0.037 | －0．227 | 10.812 | 0.004 |
| 1 | 1 I | 3 | 0.007 | 0.122 | 10.815 | 0.013 |
| 1 | H | 4 | －0．023 | －0．099 | 10：842 | 0.028 |
| 1 E1 | 18 | 5 | 0.169 | 0.308 | 12.403 | 0.030 |
|  | 1 11 | 6 | 0.377 | 0.193 | 20.400 | 0.002 |
| 151 | 1 ［1 | 7 | 0.202 | －0．080 | 22.754 | 0.002 |
| 111 | 13 | 8 | 0.052 | 0.059 | 22.916 | 0.003 |
| 1 | 1 明 | 9 | －0．030 | －0．098 | 22.970 | 0.006 |
| 1 E | 1 II | 10 | －0．129 | －0．078 | 24.000 | 0.008 |
| 14 | 10 | 11 | －0．067 | －0．072 | 24.291 | 0.012 |
| $1$ | 1 1 | 12 | －0．035 | －0．159 | 24.374 | 0.018 |
| 11 | 1 | 13 | －0．069 | －0．030 | 24.698 | 0.025 |
| 18 | 1 1 | 14 | －0．054 | －0．049 | 24.898 | 0.036 |
|  | 111 | 15 | －0．0．49 | 0.035 | 25.068 | 0.049 |
| 1 | 1 1 | 16 | －0．049 | 0.058 | 25.243 | 0.066 |
| 1 | 101 | 17 | －0．007 | 0.065 | 25.247 | 0.089 |
| 1 | 111 | 18 | －0．037 | 0.025 | 25.358 | 0.115 |
| 10 | $1] 1$ | 19 | －0．062 | 0.027 | 25.674 | 0.140 |
| 14 | 1 | 20 | －0．054 | －0．024 | 25.924 | 0．168 |

Figure ： 8.7
Correlogram of Variance of VAR Residuals，

$$
u_{21}
$$

| Included observatio | 47 | Sample：1993：2 2006：1 |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Autocorrelation | Partial Correlation | AC PAC | Q－Stat | Prob |
| 1 角 | $1 \beta$ | 10.0490 .049 | 0.1224 | 0.726 |
| 1. | 10 | $2-0.091-0.094$ | 0.5454 | 0.761 |
| 15 | 1 | $3-0.071-0.062$ | 0.8072 | 0.848 |
| 1 洨 | 1 园 | $4 \begin{array}{llll}4 & 0.176 & 0.177\end{array}$ | 2.4662 | 0.651 |
| 1 11 | 18 | 50.0920 .064 | 2.9283 | 0.711 |
|  | 1 | $6-0.0030 .013$ | 2.9289 | 0.818 |
| 1 ${ }^{\text {E }}$ | 1 ［ ${ }^{\text {d }}$ | 7 －0．125－0．095 | 3.8339 | 0.799 |
| 1 |  | $8 \quad 0.032 \quad 0.025$ | 3.8952 | 0.866 |
| $11$ | 1 团 | 9－0．047－0．096 | 4.0265 | 0.910 |
| $1 \text { 1 }$ | 1 1 | 10－0．135－0．155 | 5.1543 | 0.881 |
| E | 1 的 1 | $11-0.138-0.105$ | 6.3735 | 0.847 |
| 1 1 | 1 － 1 | $12-0.096-0.122$ | 6.9820 | 0.859 |
| 181 | ， | $13-0.111-0.137$ | 7.8218 | 0.855 |
| 1 －1 | 111 | $14 \quad 0.034 \quad 0.054$ | 7.9003 | 0.894 |
| 1 － 1 |  | $150.208 \quad 0.280$ | 11.024 | 0.751 |
|  | $1{ }^{1}$ | $16-0.200-0.200$ | 13.988 | 0.600 |
| $11$ | 1 | $17 \quad 0.031 \quad 0.155$ | 14.062 | 0.663 |
| 11 | 151 | 180.0140 .005 | 14.078 | 0.724 |
| 1 1 | 181 | $190.064-0.092$ | 14.414 | 0.759 |
|  | 14 | $20-0.031-0.074$ | 14.499 | 0.804 |

The Figures show that
i. The $A C F$ and $P A C F$ of the variance of $\hat{u_{1}}$ series contain singularly significant spike at lag one.
ii. The $A C F$ and $P A C F$ of the variance $\hat{u_{21}}$, series are free from any significant spikes at any lag.

These observations indicate that
i. Variance of the residuals $\hat{u_{1}}$ defines an $\operatorname{ARMA}(0,1)$ process, and
ii. Variance of the residuals $\hat{u_{2}}$, defines an $\operatorname{ARMA}(0,0)$ process.

Consequently, the VAR residuals, $\hat{u_{1 \prime}}$ and $\hat{u_{21}}$ are found to be free from Autoregressive Conditional Heteroscadasticity (ARCH).

### 8.13 Findings From the VAR Model (Table 8.2)

In the estimated equation (8.1) in the Table 8.2
i. $\sum_{i=1}^{4} \hat{\beta}_{i i}<1, \sum_{i=1}^{4} \hat{\gamma}_{1 i}<1$. So the autoregressive and distributed lag structures are consistent.
ii. $\hat{\beta_{11}}$ and $\hat{\beta_{12}}$ are significant at $1 \%$ and $5 \%$ levels respectively.
iii. $-1<\hat{\beta}_{11}<0$ and $-1<\hat{\beta}_{12}<0$.
iv. $\hat{\gamma_{14}}$ is significant at $5 \%$ level.

### 8.14 Economic Interpretations of Findings in Section 8.13

The economic significance of the findings in Section 8.13 is as follows:
a. Negative and significant value of $\hat{\beta}_{11}$ and $\hat{\beta}_{12}$ indicate that variations in current exchange rate were inversely related to those in one and two period back exchange rates. It again implies that variations in exchange rate beyond the second lag period failed to exert any significant effect on current exchange rate.
b. Again the negative and significant values of $\hat{\beta}_{11}$ and $\hat{\beta}_{12}$ imply that a rise(fall) in Rupee/ Nepalese Rupee Exchange rate at any period led to a fall (rise) in the exchange rate in the next period (quarter). This feature of exchange rate dynamics is a pointer to the existence of a check on the run-away appreciation/depreciation of Indian Rupee against Nepalese Rupee over the period of study. This feature of exchange rate dynamics testifies for the 'Overshooting' of $\mathrm{E}_{\mathrm{t}}$ over the period of study.
c. $\quad \gamma_{14}$ being significant, even in the presence of $\mathrm{E}_{\mathrm{t}-\mathrm{i}}(\mathrm{i}=1,2,3,4)$ in the vector of regressors in the VAR equation for $\mathrm{E}_{\mathrm{t}}$, indicates that relative price level 'Granger Caused' exchange rate over the period of study.

### 8.15 Findings From the Estimated VAR Model (Table 8.3)

It is observe from the estimated equation (8.2) in the VAR model as given in the Table 8.3 that

$$
\text { i. } \quad \sum_{i=1}^{ \pm} \hat{\beta}_{2 i}<1, \sum_{i=1}^{4} \hat{\gamma}_{2 i}<1 \quad i=1,2,3,4
$$

So the autoregressive and distributed lag structures are consistent.
ii. $\quad \hat{\beta}_{2 i}(i=1, \ldots \ldots . . ., 4)$ are not significant even at $10 \%$ level.
iii. $\quad \hat{\gamma_{24}}$ is significant at $1 \%$ level.
iv. $0<\hat{\gamma_{24}}<1$.

### 8.16 Economic Interpretations of the Findings in Section 8.15

Economic significance of the findings from the estimated equation (8.2) as given in Section 8.15 is as follows.
(a) $\hat{\gamma}_{24}$, being significant and positive, indicates that current relative price level was positively related to those in past fourth quarter. This is a pointer to the fact that the
relative price level (for India and Nepal) exhibited a sustained trend over the subperiod concerned.
(b) again $0<\hat{\gamma_{24}}<1$ indicates that in the quarterly dataset, variations in four quarter back relative price level affect the current quarter relative price level directly, nonproportionately.

As a matter of fact, this feature accounts for a declining spell of relative price level over the sub-period concerned. This feature owes its emergence to a lower inflationary rate in India than that in Nepal over the period 1993:2-2006:1.
(c) $\hat{\beta}_{2 i}(i=1, \ldots \ldots . .4)$ are not statistically significant in the presence of $\mathrm{P}_{\mathrm{t}-\mathrm{i}}(\mathrm{i}=1, \ldots 4)$ in the vector of regressors for the $P_{t}$ equation (equation 8.2) in the VAR model. This indicates that exchange rate 'failed to Granger Cause' relative price level over the sub-period concerned.
(d) $\hat{\beta}_{2 i}(i=1, \ldots \ldots . .4$ 4) being insignificant even at $10 \%$ level indicate that relative price level $\left(\mathrm{P}_{\mathrm{t}}\right)$ is an exogenous variable in the VAR model. Consequently, relative price level $\left(P_{t}\right)$ in the economy of India and Nepal appeared to be determined by some other factors than exchange rate. Exchange rate variations, therefore, 'failed to Granger Cause' variations in relative price level over the period 1993:2-2006:1.

### 8.17 Summary of Findings in Chapter 8

It is, therefore, observed in Section 8.13 through Section 8.16 that over the sub-period 1993:2-2006:1.
i. relative price level 'Granger Caused' exchange rate.
ii. exchange rate 'failed to Granger Cause' relative price level.
iii. there did exist, therefore, 'Uni-Directional Causality' running from relative price level to exchange rate.
iv. Relative price level appeared to be an exogenous variable in the VAR model (i.e in the system).

